

4 Given that  $f(x) = x^4 - 1$ :

(a) write down the value of  $f(-1)$ ; (1 mark)

(b) show that  $f(-1 + h) = -4h + 6h^2 - 4h^3 + h^4$ ; (3 marks)

(c) hence find the value of  $f'(-1)$ . (2 marks)

4(a)	$f(-1) = 0$	B1	1	M1 for two correct terms ag convincingly shown
(b)	$(-1 + h)^4 = 1 - 4h + 6h^2 - 4h^3 + h^4$ Hence result	M1A1 A1	3	
(c)	$\frac{f(-1 + h) - f(-1)}{(-1 + h) - (-1)} = -4 + \text{terms in } h$	M1		
	So $f'(-1) = -4$	A1	2	
<b>Total</b>			<b>6</b>	

4 The function  $f$  is defined for all real values of  $x$  by

$$f(x) = x^3 + x$$

(a) Express  $f(2 + h) - f(2)$  in the form

$$ph + qh^2 + rh^3$$

where  $p$ ,  $q$  and  $r$  are integers.

(5 marks)

(b) Use your answer to part (a) to find the value of  $f'(2)$ .

(2 marks)

<b>4(a)</b>	$(2 + h)^3 = 8 + ah + bh^2 + h^3$ $(2 + h)^3 = 8 + 12h + 6h^2 + h^3$ $f(2 + h) - f(2) = 13h + 6h^2 + h^3$	M1 A1A1 m1A1F	5	A1 for each of $a, b$ ; PI Ft one coeff. wrong
<b>(b)</b>	Divide by $h$ and let $h \rightarrow 0$ $f'(2) = p = 13$	M1 A1F	2	NMS B1F ft wrong value of $p$
	<b>Total</b>		<b>7</b>	

4 For each of the following improper integrals, find the value of the integral **or** explain briefly why it does not have a value:

(a)  $\int_2^{\infty} 8x^{-3} dx;$  (3 marks)

(b)  $\int_2^{\infty} (8x^{-3} + 1) dx;$  (1 mark)

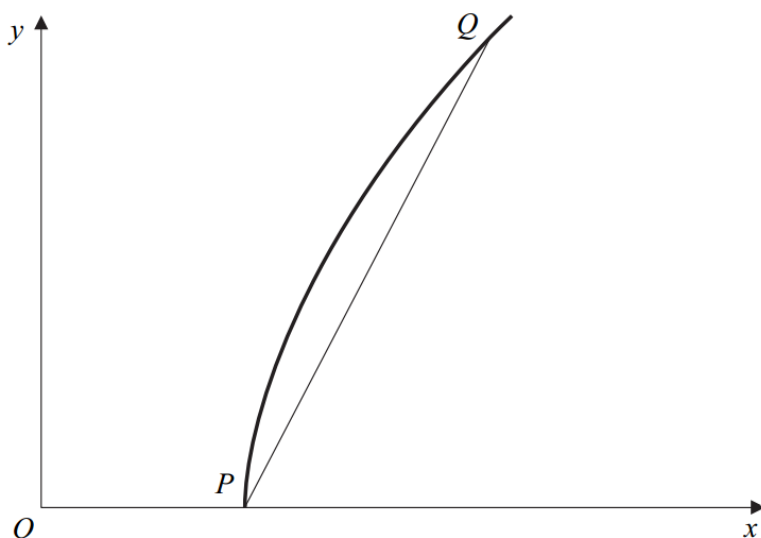
(c)  $\int_2^{\infty} 8x^{-3}(x + 1) dx.$  (3 marks)

Q	Solution	Marks	Totals	Comments
4(a)	$\int x^{-3} dx = kx^{-2} (+c)$	M1		OE
	$x^{-n} \rightarrow 0$ as $x \rightarrow \infty$	M1		
	Improper integral has value 1	A1	3	
(b)	No value as $x$ term tends to $\infty$	B1	1	
(c)	$\int x^{-2} dx = kx^{-1} (+c)$	M1		
	$x^{-1} \rightarrow 0$ as $x \rightarrow \infty$	m1		
	Improper integral has value 5	A1	3	
	<b>Total</b>		<b>7</b>	

8 The diagram shows a part of the curve

$$\frac{x^2}{4} - \frac{y^2}{6} = 1$$

and a chord  $PQ$  of the curve, where  $P$  lies on the  $x$ -axis.



(a) Write down the coordinates of  $P$ . (1 mark)

(b) The gradient of the chord  $PQ$  is 2. Find the coordinates of  $Q$ . (7 marks)

<b>8(a)</b>	$P$ is $(2, 0)$	B1	1	
<b>(b)</b>	$PQ$ is $y = 2(x - 2)$ Elimination of $y$ (or of $x$ ) $(x - 2)(5x - 22) = 0$ $Q$ is $(4.4, 4.8)$	M1A1F m1A1F A1 A1A1	7	ft wrong value for $x_p$ ft numerical error
	<b>Total</b>		<b>8</b>	

