

2. A car of mass 1000 kg is towing a caravan of mass 750 kg along a straight horizontal road. The caravan is connected to the car by a tow-bar which is parallel to the direction of motion of the car and the caravan. The tow-bar is modelled as a light rod. The engine of the car provides a constant driving force of 3200 N. The resistances to the motion of the car and the caravan are modelled as constant forces of magnitude 800 newtons and  $R$  newtons respectively.

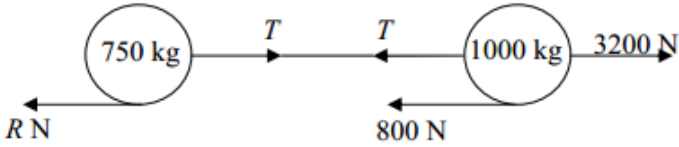
Given that the acceleration of the car and the caravan is  $0.88 \text{ m s}^{-2}$ ,

- (a) show that  $R = 860$ ,

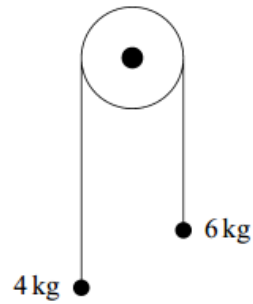
(3)

- (b) find the tension in the tow-bar.

(3)

Question Number	Scheme	Marks
<p><b>2 (a)</b></p>	 <p>For the whole system  <math>R(\rightarrow) \quad 3200 - 800 - R = 1750 \times 0.88</math>            Leading to <math>R = 860 \text{ *}</math></p>	<p>M1 A1            A1            (3)</p>
<p><b>(b)</b></p>	<p>For the caravan  <math>R(\rightarrow) \quad T - 860 = 750 \times 0.88</math>            Leading to <math>T = 1520 \text{ (N)}</math></p>	<p>M1 A1            A1            (3)</p>
<p><i>Alternative for (b)</i>            For the car  <math>R(\rightarrow) \quad 3200 - 800 - T = 1000 \times 0.88</math>            Leading to <math>T = 1520 \text{ (N)}</math></p>		<p>M1 A1            A1            (3)</p>

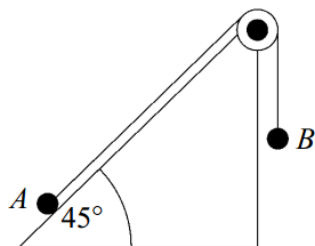
- 3 Two particles, of masses 4 kg and 6 kg, are connected by a light, inextensible string that passes over a smooth, light pulley. The two particles are released from rest, with the string taut, as shown in the diagram.



- (a) Show that the acceleration of each particle is  $1.96 \text{ m s}^{-2}$ . (5 marks)
- (b) Calculate the tension in the string. (2 marks)

3(a)	$T - 4g = 4a$ $6g - T = 6a$ $6g - (4a + 4g) = 6a$ $a = \frac{2g}{10} = 1.96 \text{ m s}^{-2}$	M1 A1 A1  m1 A1	5	Forms two equations of motion First equation correct Second equation correct  Solves for $a$ Correct $a$ from correct working
(b)	$T = 4 \times 1.96 + 4 \times 9.8 = 47.0 \text{ N}$	M1 A1	2	Uses one equation to find $T$ Correct $T$
<b>Total</b>			<b>7</b>	

- 4 Two particles,  $A$  and  $B$ , are connected by a light inextensible string, which passes over a smooth light pulley. Particle  $A$  is on a smooth slope, at  $45^\circ$  to the horizontal, and particle  $B$  hangs with the string vertical, as shown in the diagram.

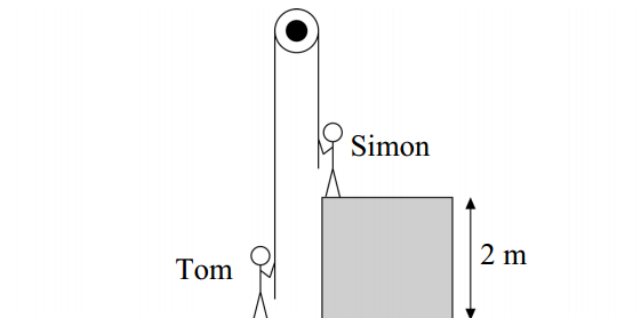


The mass of  $A$  is 14 kg and the mass of  $B$  is 6 kg.

- (a) Using two equations of motion, show that the acceleration of the particles is  $1.91 \text{ m s}^{-2}$ , correct to three significant figures. (6 marks)
- (b) Particle  $B$  is replaced by a particle  $C$  of mass  $m$  kg. After the particles have been set in motion, they move with a constant speed. Find  $m$ . (4 marks)

Question Number and Part	Solution	Marks	Total	Comments
4(a)	$14a = 14g \sin 45^\circ - T$ $6a = T - 6g$ $14a = 14g \sin 45^\circ - (6a + 6g)$ $a = \frac{14g \sin 45^\circ - 6g}{20} = 1.91 \text{ ms}^{-2}$	M1 A1 M1 A1 M1 A1	6	Equation of motion for one particle Correct equation Equation of motion for other particle Correct equation Solving for $a$ Correct $a$ from correct working
(b)	$T = mg$ $T = 14g \cos 45^\circ$ $m = 14 \cos 45^\circ = 9.90 \text{ kg}$	M1 M1 A1 A1	4	Equation for one particle Equation for other particle Correct $m$
	<b>Total</b>		<b>10</b>	

- 6 Two children are holding the ends of a light, inextensible rope, which passes over a light, smooth pulley. Initially Tom, who has a mass of 40 kg, is standing on ground level and Simon, who has a mass of 60 kg, is on the edge of a fixed platform 2 metres above ground level. Model the two boys as particles, one initially at ground level, and the other initially at a height of 2 metres. The rope is taut.



Simon steps off the platform and as he falls vertically, Tom rises vertically.

- (a) Assume that the rope remains taut while the boys are moving.
- (i) Show that the acceleration of each boy is  $1.96 \text{ m s}^{-2}$ . (5 marks)
- (ii) Find the tension in the rope. (2 marks)
- (b) Find the total distance that Tom travels upwards. (7 marks)

Question Number and part	Solution	Marks	Total	Comments
6(a)(i)	$60 \times 9.8 - T = 60a$ $T - 40 \times 9.8 = 40a$ $588 - (40a + 392) = 60a$ $a = 1.96 \text{ m s}^{-2}$	M1 A1 M1 A1 A1	5	Equation of motion for one boy Correct equation Equation of motion for other boy Correct equation <b>ag</b> Correct answer from correct working
(ii)	$T = 40 \times 1.96 + 392 = 470 \text{ N (to 3 sf)}$	M1 A1	2	Substituting for $a$ and solving for $T$ awrt 470
6(b)	$v^2 = 0^2 + 2 \times 1.96 \times 2 = 7.84$ $0^2 = 7.84 + 2 \times (-9.8)s$ $s = 0.4$ $h_{\text{max}} = 2 + 0.4 = 2.4 \text{ m}$	M1 A1 m1 A1 m1 A1 A1	7	Finding $v^2$ using $s = 2$ , $u = 0$ and $a = 1.96$ Correct $v$ or $v^2$ Equation for $s$ with $v = 0$ and $a = \pm g$ Solving for $s$ Obtaining 0.4 Adding 2 to get 2.4
	<b>Total</b>		<b>14</b>	